

General Instructions

- (i) This question paper contains 22 questions. All questions are compulsory.
- (ii) It comprises 16 single-correct multiple-choice questions and 6 numerical / integer-type questions.
- (iii) Attempt every question; detailed solutions are provided in the companion solutions booklet.
- (iv) For numerical questions, report the answer rounded exactly as asked.

1. Let a_n be the n^{th} term of a decreasing infinite geometric progression. If $a_1 + a_2 + a_3 = 52$ and $a_1a_2 + a_2a_3 + a_3a_1 = 624$, then the sum of this geometric progression is:

- (A) 57
- (B) 63
- (C) 54
- (D) 60

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2. Two tangents drawn from a point P touch a circle with center O at points Q and R . Points A and B lie on PQ and PR , respectively, such that AB is also a tangent to the same circle. If $\angle AOB = 50^\circ$, then $\angle APB$, in degrees, equals:

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3. Let $ABCDEF$ be a regular hexagon and P and Q be the midpoints of AB and CD , respectively. Then, the ratio of the areas of trapezium $PBCQ$ and hexagon $ABCDEF$ is:

- (A) 6 : 19
- (B) 5 : 24
- (C) 6 : 25
- (D) 7 : 24

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4. Suppose a, b, c are three distinct natural numbers, such that $3ac = 8(a + b)$. Then, the smallest possible value of $3a + 2b + c$ is:

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5. The ratio of expenditures of Lakshmi and Meenakshi is 2 : 3, and the ratio of income of Lakshmi to expenditure of Meenakshi is 6 : 7. If excess of income over expenditure is saved by Lakshmi and Meenakshi, and the ratio of their savings is 4 : 9, then the ratio of their incomes is:

- (A) 7 : 8
- (B) 3 : 5
- (C) 2 : 1
- (D) 5 : 6

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6. If $\log_{64} x^2 + \log_8 \sqrt{y} + 3 \log_{512} (\sqrt{y}z) = 4$, where x, y and z are positive real numbers, then the minimum possible value of $(x + y + z)$ is:

- (A) 24
- (B) 36
- (C) 96
- (D) 48

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7. If $9^{x^2+2x-3} - 4(3^{x^2+2x-2}) + 27 = 0$, then the product of all possible values of x is:

- (A) 2
- (B) 4
- (C) 10
- (D) 20

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8. The average number of copies of a book sold per day by a shopkeeper is 60 in the initial seven days and 63 in the initial eight days, after the book launch. On the ninth day, she sells 11 copies less than the eighth day, and the average number of copies sold per day from the second day to the ninth day becomes 66. The number of copies sold on the first day of the book launch is:

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9. A loan of Rs 1000 is fully repaid by two installments of Rs 530 and Rs 594, paid at the end of the first and second year, respectively. If the interest is compounded annually, then the rate of interest, in percentage, is:

- (A) 6
- (B) 7
- (C) 8
- (D) 9

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10. The set of all real values of x for which $(x^2 - |x + 9| + x) > 0$ is:

- (A) $(-\infty, -9) \cup (3, \infty)$
- (B) $(-\infty, -3) \cup (9, \infty)$
- (C) $(-\infty, -3) \cup (3, \infty)$
- (D) $(-9, -3) \cup (3, 9)$

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11. The equations $3x^2 - 5x + p = 0$ and $2x^2 - 2x + q = 0$ have one common root. The sum of the other roots of these two equations is:

- (A) $\frac{5}{3} - p + q$
- (B) $\frac{8}{3} + p - q$
- (C) $\frac{8}{3} - p + \frac{3}{2}q$
- (D) $p + q - 1$

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12. An item with a cost price of Rs.1650 is sold at a certain discount on a fixed marked price to earn a profit of 20% on the cost price. If the discount was doubled, the profit would have been Rs.110. The rate of discount, in percentage, at which the profit percentage would be equal to the rate of discount, is nearest to:

- (A) 12
- (B) 13
- (C) 14
- (D) 15

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13. A certain amount of money was divided among Pinu, Meena, Rinu, and Seema. Pinu received 20% of the total amount and Meena received 40% of the remaining amount. If Seema received 20% less than Pinu, the ratio of the amounts received by Pinu and Rinu is:

- (A) 4 : 5
- (B) 5 : 8
- (C) 3 : 5
- (D) 2 : 3

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14. Let $f(x) = \frac{x}{2x-1}$ and $g(x) = \frac{x}{x-1}$. Then, the domain of the function

$$h(x) = f(g(x)) + g(f(x))$$

is all real numbers except:

- (A) $\frac{1}{2}, 1, \frac{3}{2}$
- (B) $\frac{1}{2}, 1$
- (C) $-\frac{1}{2}, \frac{1}{2}, 1$
- (D) $-1, \frac{1}{2}, 1$

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15. The number of divisors of $(2^6 \times 3^5 \times 5^3 \times 7^2)$, which are of the form $(3r + 1)$, where r is a non-negative integer, is:

- (A) 42
- (B) 36
- (C) 56
- (D) 24

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16. The sum of digits of the number $(625)^{65} \times (128)^{36}$ is:

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17. Ankita is twice as efficient as Bipin, while Bipin is twice as efficient as Chandan. All three of them start together on a job, and Bipin leaves the job after 20 days. If the job got completed in 60 days, the number of days needed by Chandan to complete the job alone, is:

- (A) 240
- (B) 260
- (C) 300
- (D) 340

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18. If m and n are integers such that $(m + 2n)(2m + n) = 27$, then the maximum possible value of $2m - 3n$ is:

- (A) 9
- (B) 13
- (C) 15
- (D) 17

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19. In a $\triangle ABC$, points D and E are on the sides BC and AC , respectively. BE and AD intersect at point T such that $AD : AT = 4 : 3$, and $BE : BT = 5 : 4$. Point F lies on AC such that DF is parallel to BE . Then, $BD : CD$ is:

- (A) 15 : 4
- (B) 11 : 4
- (C) 9 : 4
- (D) 7 : 4

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20. A mixture of coffee and cocoa, 16% of which is coffee, costs Rs 240 per kg. Another mixture of coffee and cocoa, of which 36% is coffee, costs Rs 320 per kg. If a new mixture of coffee and cocoa costs Rs 376 per kg, then the quantity, in kg, of coffee in 10 kg of this new mixture is:

- (A) 2.5
- (B) 5
- (C) 4
- (D) 6

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21. Rita and Sneha can row a boat at 5 km/h and 6 km/h in still water, respectively. In a river flowing with a constant velocity, Sneha takes 48 minutes more to row 14 km upstream than to row the same distance downstream. If Rita starts from a certain location in the river, and returns downstream to the same location, taking a total of 100 minutes, then the total distance, in km, Rita will cover is:

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22. If a, b, c and d are integers such that their sum is 46, then the minimum possible value of $(a - b)^2 + (a - c)^2 + (a - d)^2$ is: