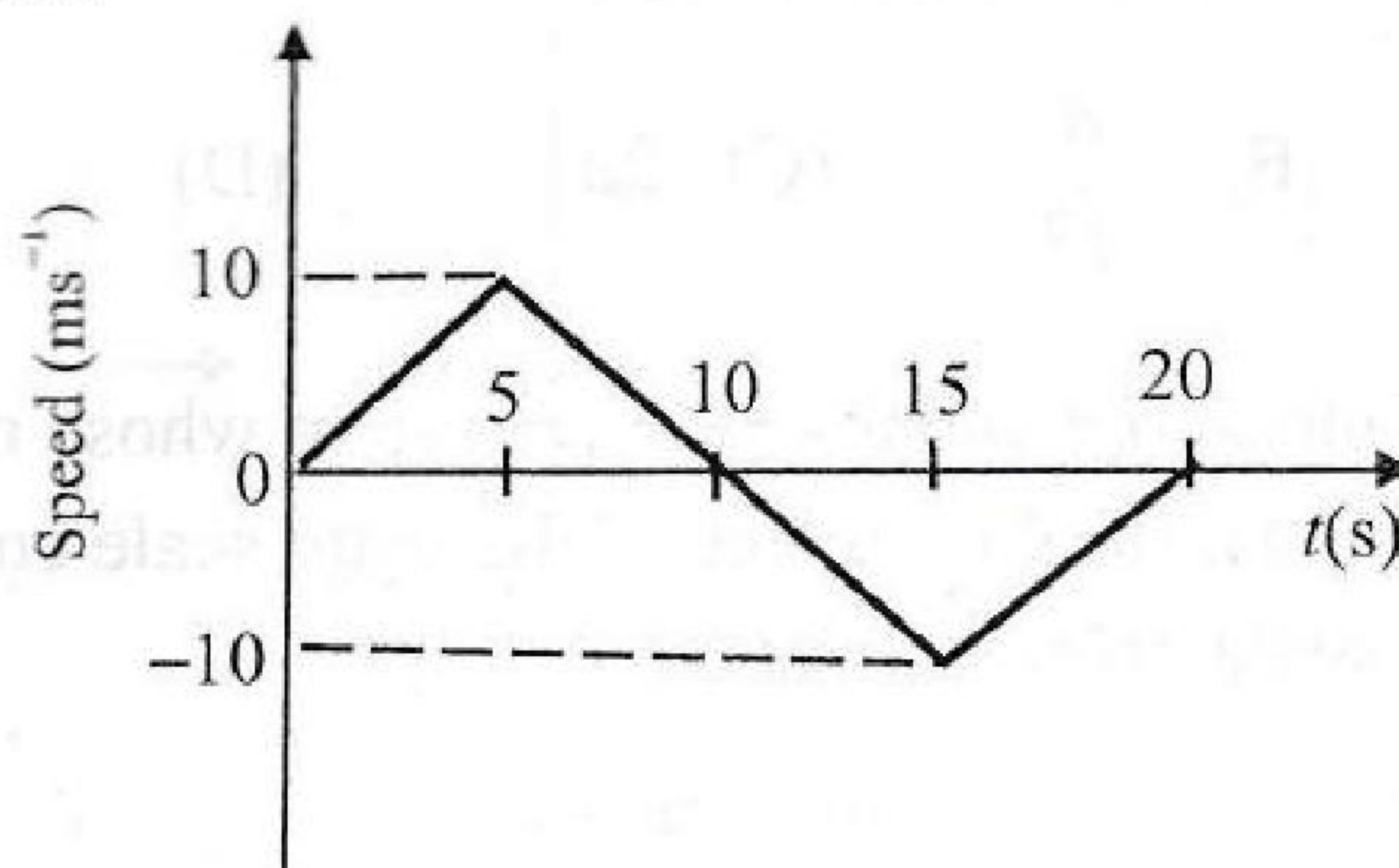


SEAL

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PLEASE ENSURE THAT THIS QUESTION BOOKLET CONTAINS
120 QUESTIONS SERIALLY NUMBERED FROM 1 TO 120.
PRINTED PAGES 32.

1. The one-dimensional motion of a point particle is shown in the figure. Select the correct statement



- (A) The total distance travelled by the particle is zero
(B) The total displacement of the particle is zero
(C) The maximum acceleration of the particle is $\frac{1}{2} \text{ ms}^{-2}$
(D) The total distance travelled by the particle at the end of 10 s is 100 m
(E) At the 5th second, the acceleration of the particle is 2 ms^{-2}

2. The period of oscillation of a simple pendulum is given by $T = 2\pi\sqrt{\frac{L}{g}}$, where L is the length of the pendulum and g is the acceleration due to gravity. The length is measured using a meter scale which has 2000 divisions. If the measured value of L is 50 cm, the accuracy in the determination of g is 1.1% and the time taken for 100 oscillations is 100 seconds, what should be the resolution of the clock (in milliseconds)?

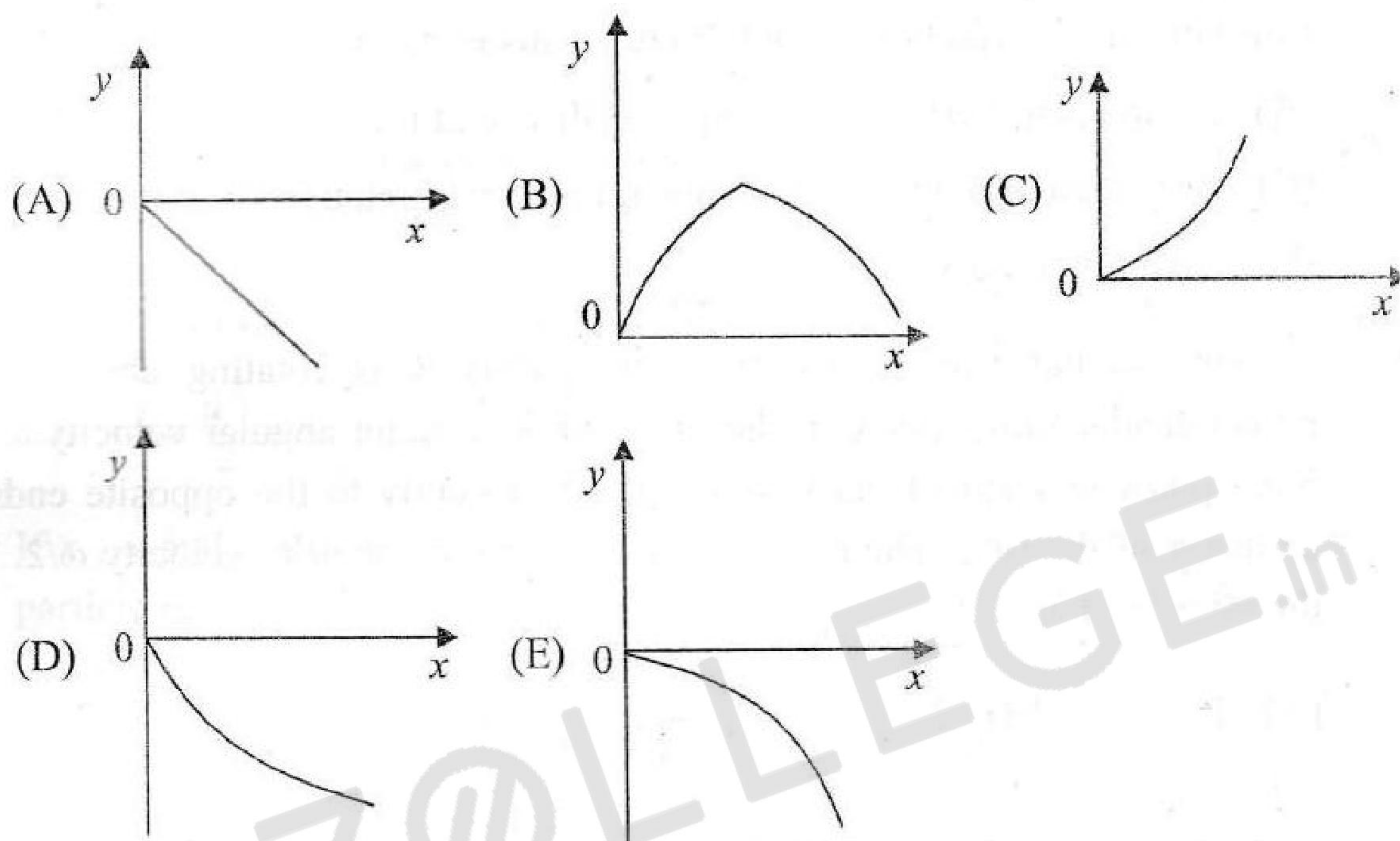
- (A) 1 (B) 2 (C) 5
(D) 0.25 (E) 0.1

Space for rough work

3. From a circular card board of uniform thickness and mass M , a square disc of maximum possible area is cut. If the moment of inertia of the square with the axis of rotation at the centre and perpendicular to the plane of the disc is $\frac{Ma^2}{6}$, the radius of the circular card board is
- (A) $\sqrt{2}a$ (B) $\frac{a}{\sqrt{2}}$ (C) $2a$ (D) $\frac{1}{2a}$ (E) $2\sqrt{2}a$
4. The length is measured using a vernier system whose main scale is 30 cm long with 600 divisions. If 19 divisions of the main scale coincide with 20 divisions of the vernier scale, then its least count is
- (A) 0.25 cm (B) 0.025 cm (C) 0.25 mm
(D) 0.025 mm (E) 0.0025 mm
5. A particle of mass m is moving along the x -axis under the potential $V(x) = \frac{kx^2}{2} + \frac{\lambda}{x}$, where k and λ are positive constants of appropriate dimensions. The particle is slightly displaced from its equilibrium position. The particle oscillates with the angular frequency ω given by
- (A) $3\frac{k}{m}$ (B) $3\frac{m}{k}$ (C) $\sqrt{\frac{k}{m}}$ (D) $\sqrt{3\frac{m}{k}}$ (E) $\sqrt{3\frac{k}{m}}$

Space for rough work

6. Two particles of mass m and $2m$ have their position vectors as a function of time as $\vec{r}_1(t) = t\hat{i} - t^3\hat{j} + 2t^2\hat{k}$ and $\vec{r}_2(t) = t\hat{i} - t^3\hat{j} - t^2\hat{k}$ respectively (where t is the time). Which one of the following graphs represents the path of the centre of mass



7. Two planets A and B have the same average density. Their radii R_A and R_B are such that $R_A : R_B = 3:1$. If g_A and g_B are the acceleration due to gravity at the surfaces of the planets, then $g_A : g_B$ equals

(A) 3 : 1 (B) 1 : 3 (C) 9 : 1 (D) 1 : 9 (E) $\sqrt{3} : 1$

Space for rough work

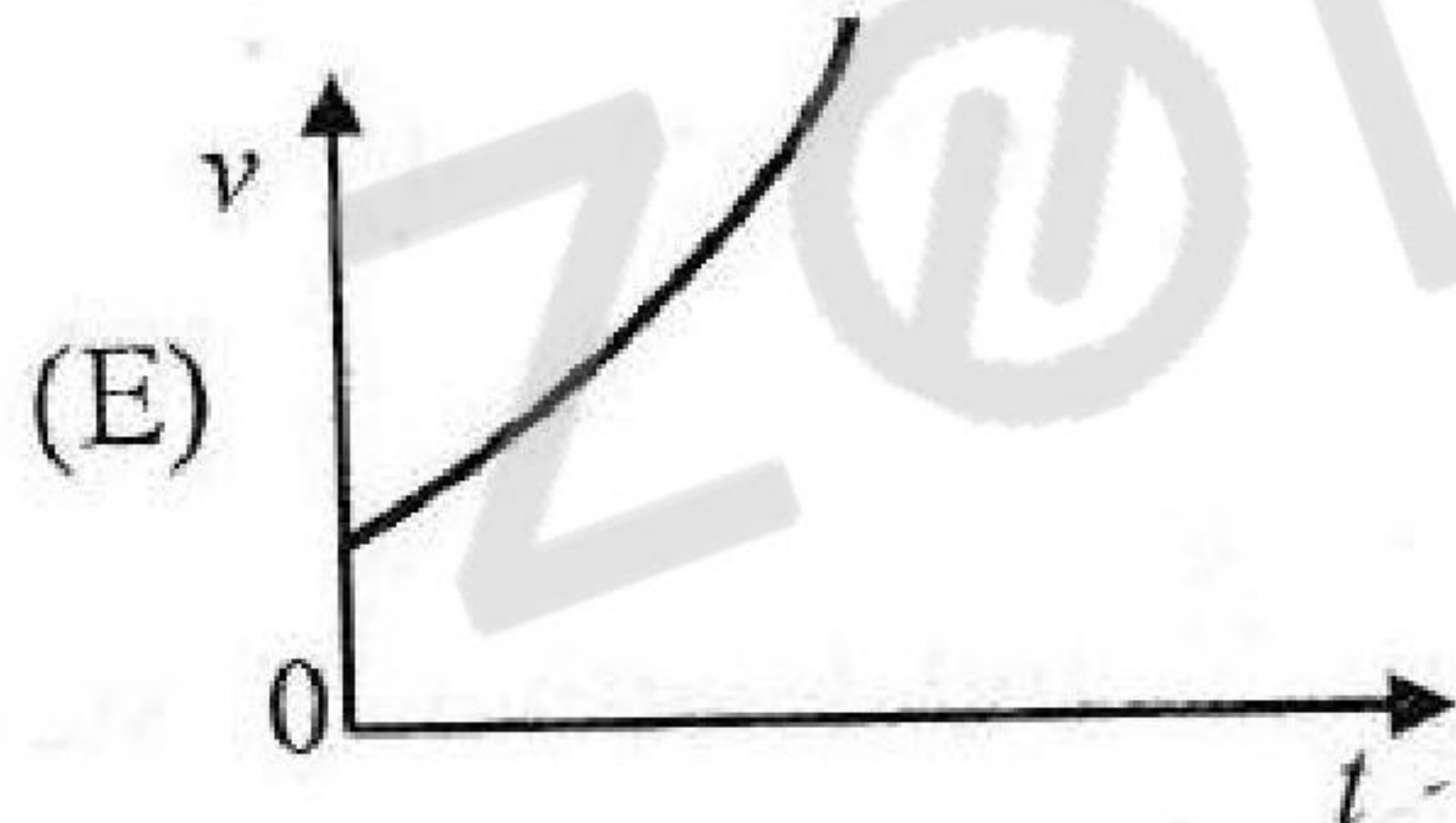
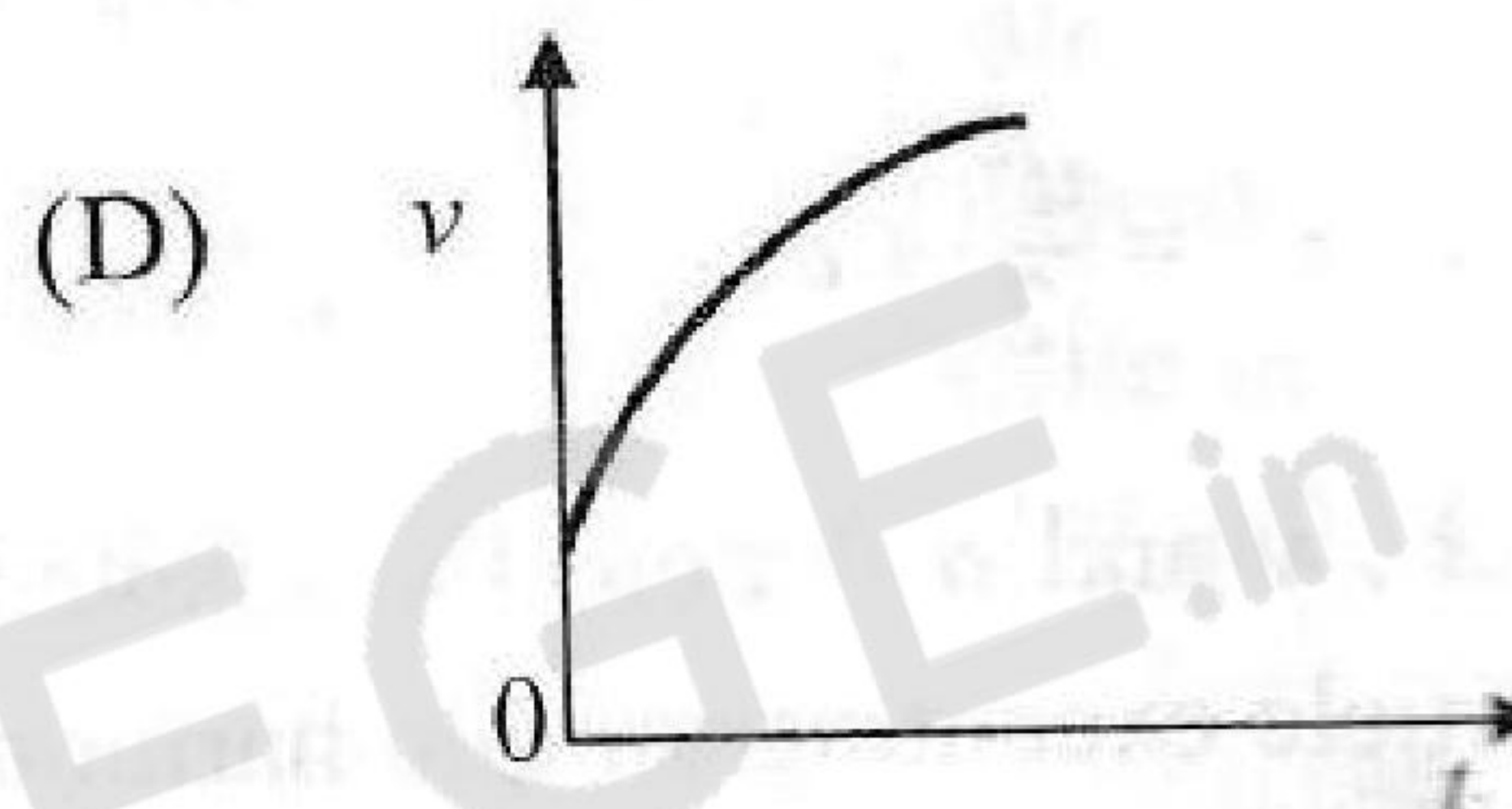
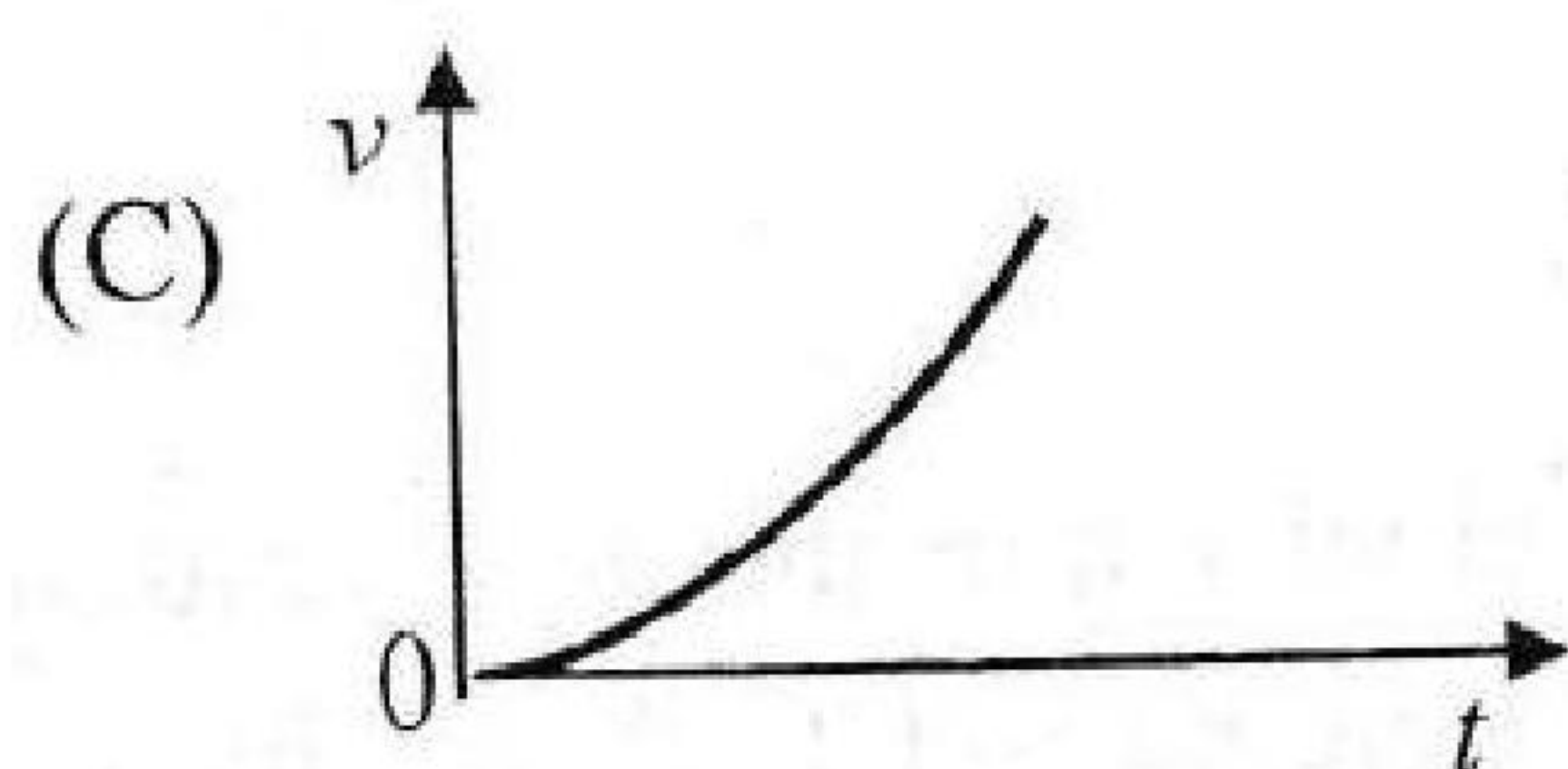
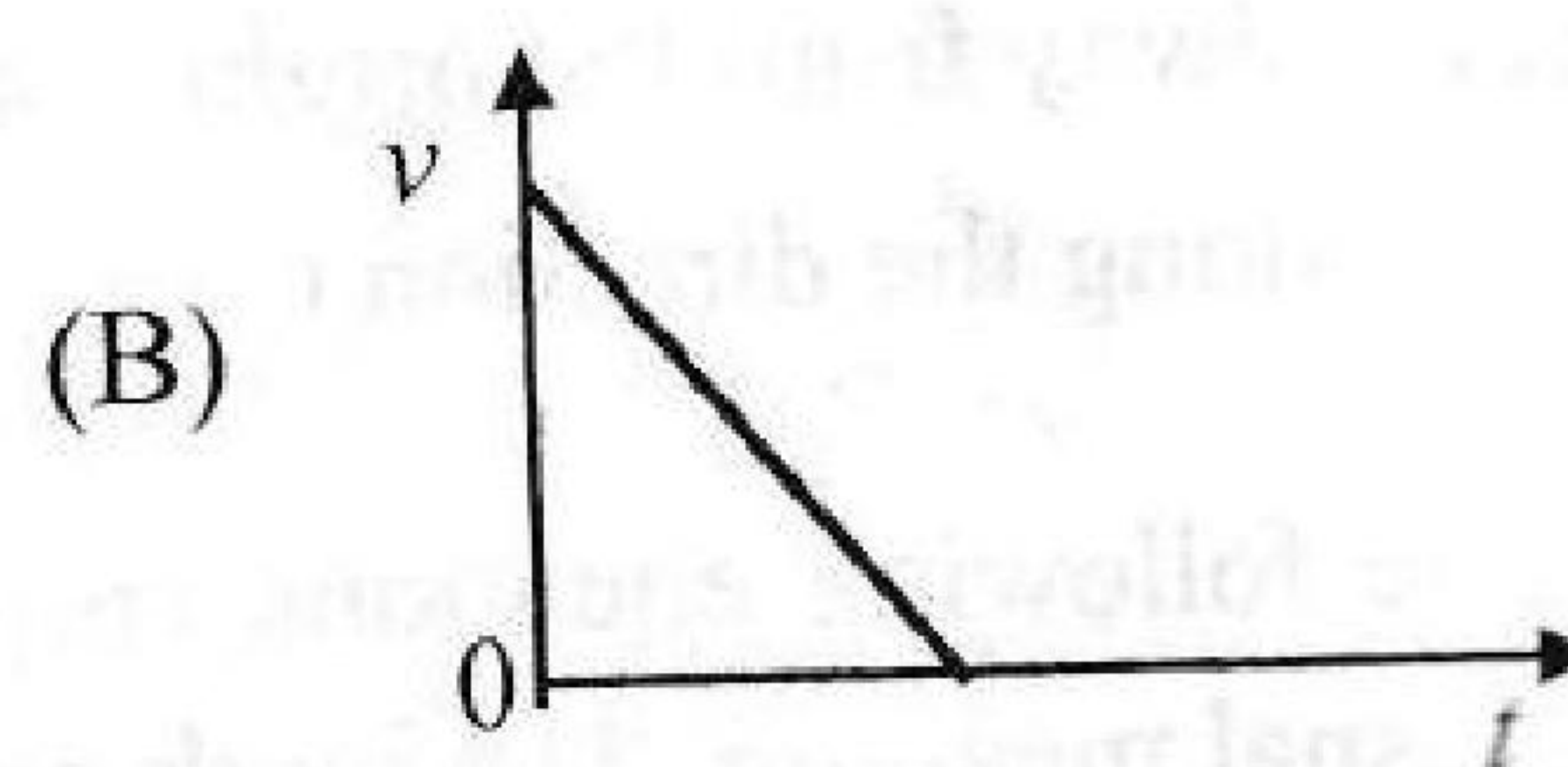
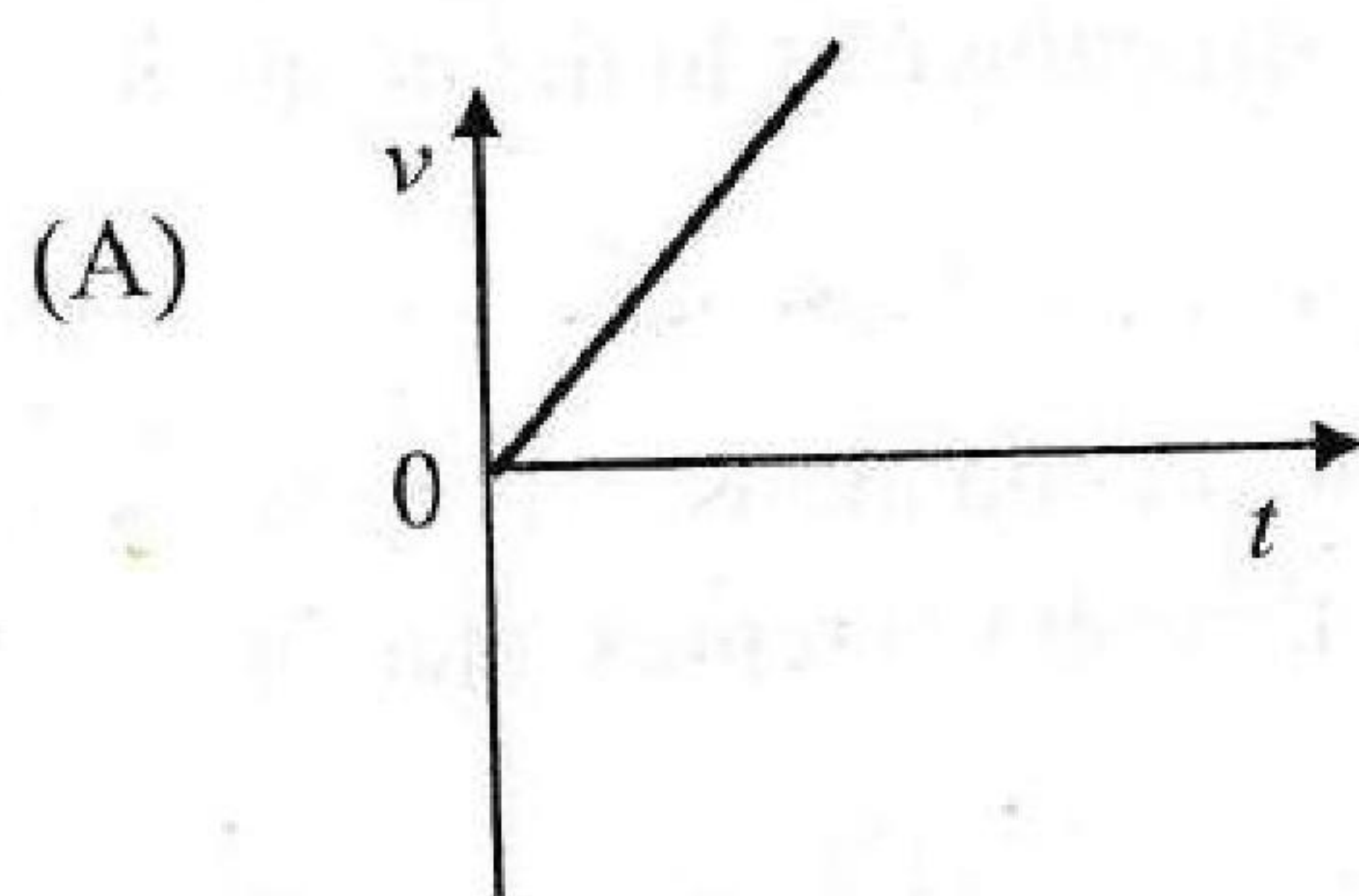
8. The magnetic induction field has the dimensions of
 (A) Force (B) Force constant (C) Surface tension
 (D) $\frac{\text{Surface tension}}{\text{Current}}$ (E) Force constant $\times$ current
9. Einstein was awarded the Nobel Prize for his work on
 (A) Photoelectric effect (B) Special theory of relativity
 (C) Brownian motion (D) General theory of relativity
 (E) Quantum theory
10. A thin circular ring of mass m and radius R is rotating about its axis perpendicular to the plane of the ring with a constant angular velocity ω . Two point particles each of mass M are attached gently to the opposite ends of a diameter of the ring. The ring now rotates with an angular velocity $\omega/2$. Then, the ratio m/M is
 (A) 1 (B) 2 (C) $\frac{1}{2}$ (D) $\sqrt{2}$ (E) $\frac{1}{\sqrt{2}}$
11. A body of mass $m = 1$ kg is moving in a medium and experiences a fractional force $F = -kv$, where v is the speed of the body. The initial speed is $v_0 = 10 \text{ ms}^{-1}$ and after 10 s, its energy becomes half of initial energy. Then, the value of k is
 (A) $10 \ln \sqrt{2}$ (B) $\ln \sqrt{2}$ (C) $\frac{\ln 2}{20}$ (D) $10 \ln 2$ (E) $\ln 2$

Space for rough work

12. The position vector of the particle is $\vec{r}(t) = a \cos \omega t \hat{i} + a \sin \omega t \hat{j}$, where a and ω are real constants of suitable dimensions. The acceleration is
 (A) perpendicular to the velocity (B) parallel to the velocity
 (C) directed away from the origin (D) perpendicular to the position vector
 (E) always along the direction of $\hat{i}$
13. Some of the following equations are kinematic equations, where the symbols have their usual meaning. The work-energy theorem is represented by
 (A) $v = u + at$ (B) $s = ut$ (C) $s = ut + \frac{1}{2}at^2$
 (D) $v^2 = \frac{u^2}{2} + as$ (E) $v^2 = u^2 + 2as$
14. If x , v and a denote the displacement, the velocity and the acceleration of a particle executing simple harmonic motion of time period T , then which of the following do not change with time?
 (A) aT/v (B) $aT + 2\pi v$ (C) $a^2T^2 + 4\pi^2v^2$
 (D) aT (E) vT
15. A rubber cord of density d , Young's modulus Y and length L is suspended vertically. If the cord extends by a length $0.5 L$ under its own weight, then L is
 (A) $\frac{Y}{2dg}$ (B) $\frac{Y}{dg}$ (C) $\frac{2Y}{dg}$ (D) $\frac{dg}{2Y}$ (E) $\frac{dg}{Y}$

Space for rough work

16. Which of the following graphs represents the speed v of a projectile as a function of time t



17. A body P floats in water with half its volume immersed. Another body Q floats in a liquid of density $\frac{3}{4}$ th of the density of water with two-third of the volume immersed. The ratio of density of P to that of Q is

(A) 1:2 (B) 1:1 (C) 2:1 (D) 2:3 (E) 3:4

Space for rough work

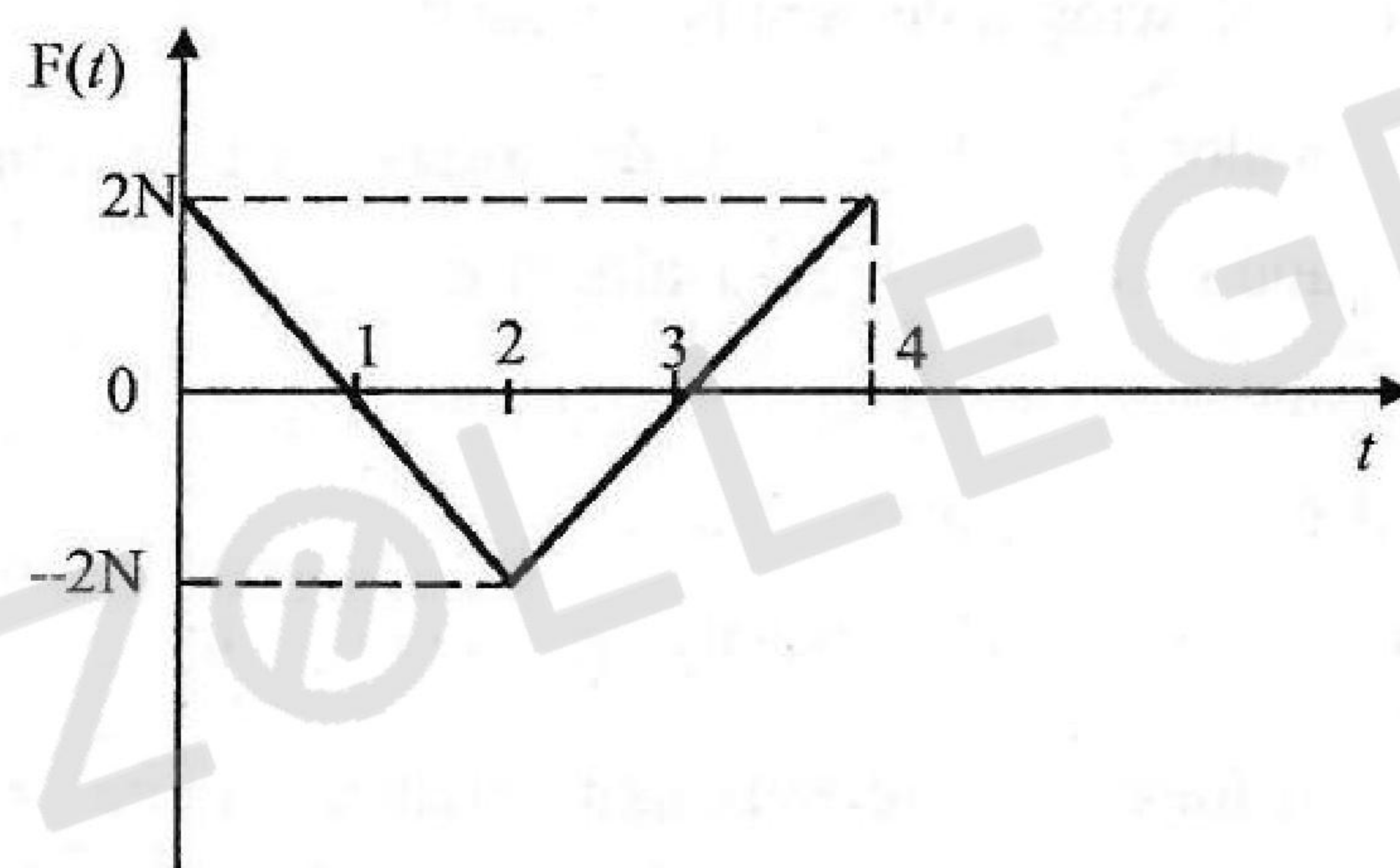
18. A pipe of 1 m length is closed at one end. Taking the speed of sound in air as 320 ms^{-1} , the air column in the pipe **cannot** resonate for the frequency (in Hz)
- (A) 80 (B) 160 (C) 240 (D) 560 (E) 720
19. A wave pulse in a string is described by the equation $y_1 = \frac{5}{(3x-4t)^2 + 2}$ and another wave pulse in the same string is described by $y_2 = \frac{-5}{(3x+4t-6)^2 + 2}$. The values of y_1 , y_2 and x are in meters and t in seconds. Which of the following statement is correct ?
- (A) y_1 travels along $-x$ -direction and y_2 along $+x$ -direction
 (B) both y_1 and y_2 travel along $-x$ -direction
 (C) both y_1 and y_2 travel along $+x$ -direction
 (D) at $x = 1 \text{ m}$, y_1 and y_2 always cancel
 (E) at time $t = 1 \text{ s}$, y_1 and y_2 exactly cancel everywhere
20. The maximum transverse velocity and maximum transverse acceleration of a harmonic wave in a one-dimensional string are 1 ms^{-1} and 1 ms^{-2} respectively. The phase velocity of the wave is 1 ms^{-1} . The waveform is
- (A) $\sin(x-t)$ (B) $\sin(2x-t)$ (C) $\sin(x-2t)$
 (D) $\sin(x/2-t)$ (E) $\sin(x-t/2)$
21. Two particles A and B of same mass have their de Broglie wavelengths in the ratio $\lambda_A : \lambda_B = k : 1$. Their potential energies $U_A : U_B = 1 : k^2$. The ratio of their total energies $E_A : E_B$ is
- (A) $k^2 : 1$ (B) $1 : k^2$ (C) $k : 1$ (D) $1 : k$ (E) $1 : 1$

Space for rough work

22. A particle is moving along the x -axis such that its acceleration is proportional to the displacement from the equilibrium position and they are in the same direction. The displacement $x(t)$ is given by

(A) $\sin \omega t, \omega > 0$ (B) $\sin \omega t + \cos \omega t, \omega > 0$ (C) $e^{\omega t}, \omega > 0$
 (D) $e^{\omega t} + \sin \omega t, \omega > 0$ (E) $e^{\omega_1 t} + e^{-\omega_2 t}, \omega_1 \text{ and } \omega_2 > 0$

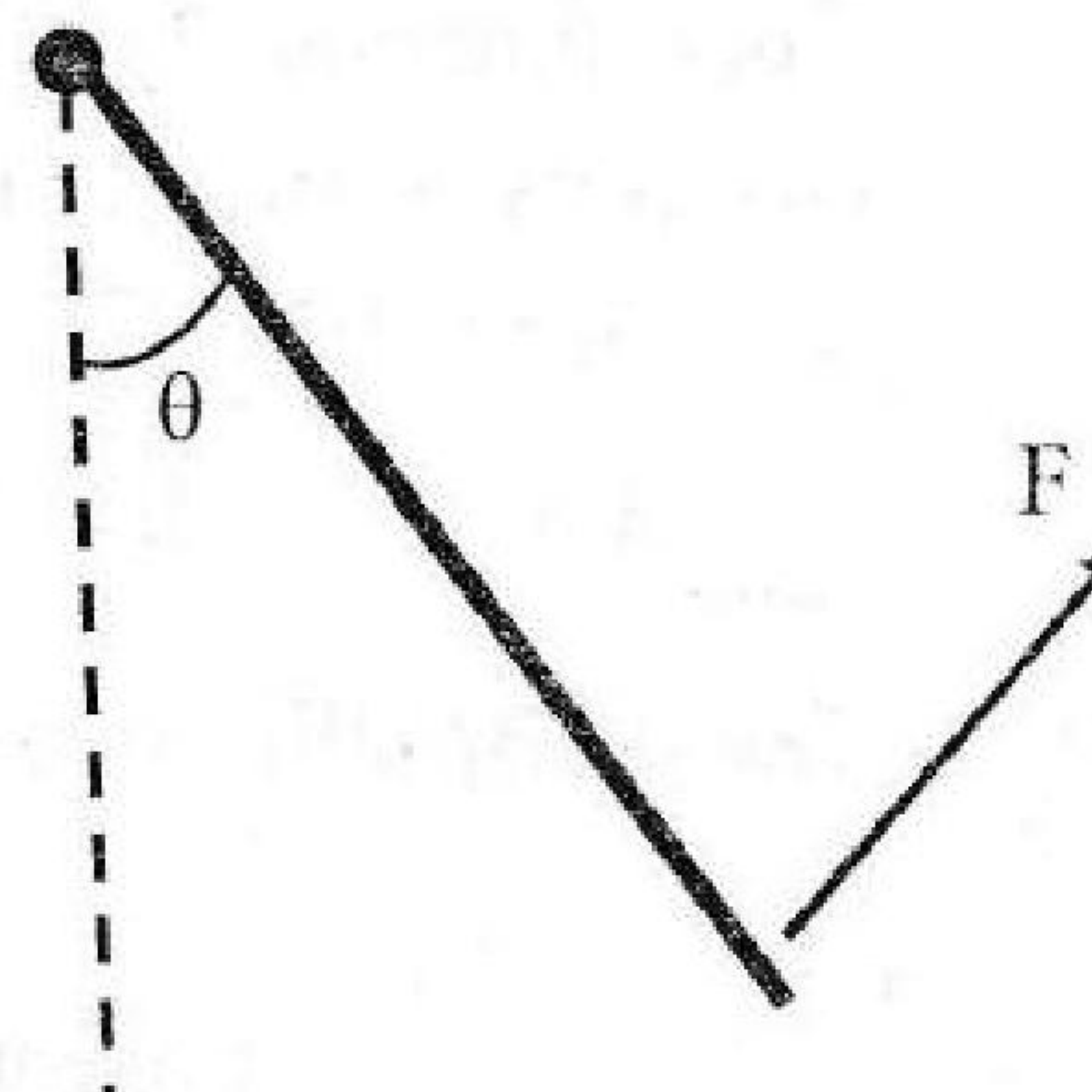
23. A block of mass 1 kg is free to move along the x -axis. It is at rest and from time $t = 0$ onwards it is subjected to a time-dependent force $F(t)$ in the x -direction. The force $F(t)$ varies with t as shown in figure. The kinetic energy of the block at $t = 4$ s is



- (A) 1 J (B) 2 J (C) 3 J (D) 0 J (E) 4 J
24. Consider a wire with density ρ and stress σ . For the same density, if the stress increases 2 times, the speed of the transverse waves along the wire changes by
- (A) $\sqrt{2}$ (B) $\frac{1}{\sqrt{2}}$ (C) 2 (D) $\frac{1}{2}$ (E) 4

Space for rough work

25. Two soap bubbles of radii 3 mm and 4 mm confined in vacuum coalesce isothermally to form a new bubble. The radius of the bubble formed (in mm) is
 (A) 3 (B) 3.5 (C) 4 (D) 5 (E) 7
26. An oscillator circuit contains an inductor 0.05 H and a capacitor of capacity 80 μF . When the maximum voltage across the capacitor is 200 V, the maximum current (in amperes) in the circuit is
 (A) 2 (B) 4 (C) 8 (D) 10 (E) 16
27. The displacement y of a particle is given by $y = 4\cos^2(t/2) \sin(1000 t)$. This expression may be considered to be a result of the superposition of how many simple harmonic motions?
 (A) 4 (B) 3 (C) 2 (D) 5 (E) 6
28. A cylindrical tube, open at both the ends has fundamental frequency n . If one of the ends is closed, the fundamental frequency will become
 (A) $\frac{n}{2}$ (B) $2n$ (C) n (D) $4n$ (E) $3n$
29. A uniform bar of mass m is supported by a pivot at its top about which the bar can swing like a pendulum. If a force F is applied perpendicular to the lower end of the bar as shown in figure, what is the value of F in order to hold the bar in equilibrium at an angle θ from the vertical



- (A) $2mg \sin \theta$ (B) $mg \sin \theta$ (C) $mg \cos \theta$
 (D) $\frac{mg}{2} \sin \theta$ (E) $\frac{mg}{2} \cos \theta$

Space for rough work

35. In a thermodynamic system, Q represents the energy transferred to or from a system by heat and W represents the energy transferred to or from a system by work.

I. $Q > 0$ and $W = 0$

II. $Q < 0$ and $W = 0$

III. $W > 0$ and $Q = 0$

IV. $W < 0$ and $Q = 0$

Which of the above will lead to an increase in the internal energy of the system?

(A) I only

(B) II only

(C) I and IV only

(D) II and III only

(E) II and IV only

36. A cylinder closed at both ends is separated into two equal parts (45 cm each) by a piston impermeable to heat. Both the parts contain the same masses of gas at a temperature of 300 K and a pressure of 1 atm. How much the gas should be heated in one part of the cylinder to shift the piston by 5 cm and the pressure of the gas after shifting the piston?

(A) $T = 365$ K and $P = 1.125$ atm

(B) $T = 350$ K and $P = 1.125$ atm

(C) $T = 375$ K and $P = 2.125$ atm

(D) $T = 350$ K and $P = 2.125$ atm

(E) $T = 375$ K and $P = 1.125$ atm

37. Five moles of an ideal monatomic gas with an initial temperature of 150°C expand and in the process absorb 1500 J of heat and does 2500 J of work. The final temperature of the gas in $^\circ\text{C}$ is (Ideal gas constant $R = 8.314 \text{ J K}^{-1} \text{ mol}^{-1}$)

(A) 134

(B) 126

(C) 144

(D) 166

(E) 174

Space for rough work

67. A radio transmitter sends out 60 W of radiation. Assuming that the radiation is uniform on a sphere with the transmitter at its centre, the intensity (in W/m^2) of the wave at a distance 12 km is
- (A) 5.33×10^{-8} (B) 3.33×10^{-6} (C) 2.12×10^{-8}
(D) 6.66×10^{-8} (E) 3.33×10^{-8}
68. Consider a system of gas of a diatomic molecule in which the speed of sound at 0°C is 1260 ms^{-1} . Then, the molecular weight of the gas is (Given the gas constant R is 8.314 J/mol.K)
- (A) 2g (B) 2mg (C) 4g (D) 10g (E) 20g
69. A satellite is orbiting the earth in a circular orbit of radius R . Which one of the following statements is **true** ?
- (A) Angular momentum varies as $\frac{1}{\sqrt{R}}$
(B) Linear momentum varies as $\sqrt{R}$
(C) Frequency of revolution varies as $\frac{1}{R^2}$
(D) Kinetic energy varies as $\frac{1}{R}$
(E) Potential energy varies as R

Space for rough work

70. The magnitude of a magnetic field at the centre of a circular coil of radius R , having N turns and carrying a current I can be doubled by changing
- (A) I to $2I$ and N to $2N$ keeping R unchanged
 - (B) N to $\frac{N}{2}$ and keeping I and R unchanged
 - (C) N to $2N$ and R to $2R$ keeping I unchanged
 - (D) R to $2R$ and I to $2I$ keeping N unchanged
 - (E) I to $2I$ and keeping N and R unchanged
71. An alternating voltage $V = V_0 \sin \omega t$ is applied across a circuit and as a result, a current $I = I_0 \sin \left(\omega t + \frac{\pi}{2} \right)$ flows in it. The power consumed per cycle is
- (A) $I_0 V_0$
 - (B) $0.5 I_0 V_0$
 - (C) $0.7 I_0 V_0$
 - (D) $1.414 I_0 V_0$
 - (E) Zero
72. An electromagnetic wave of intensity I is incident on a non-reflecting surface. If C is the speed of light in free space, then, the ratio $\frac{I}{C}$ is same as
- (A) momentum
 - (B) force
 - (C) pressure
 - (D) pressure per unit area
 - (E) force $\times$ area

Space for rough work

