

GATE 1994 EC Answer Key

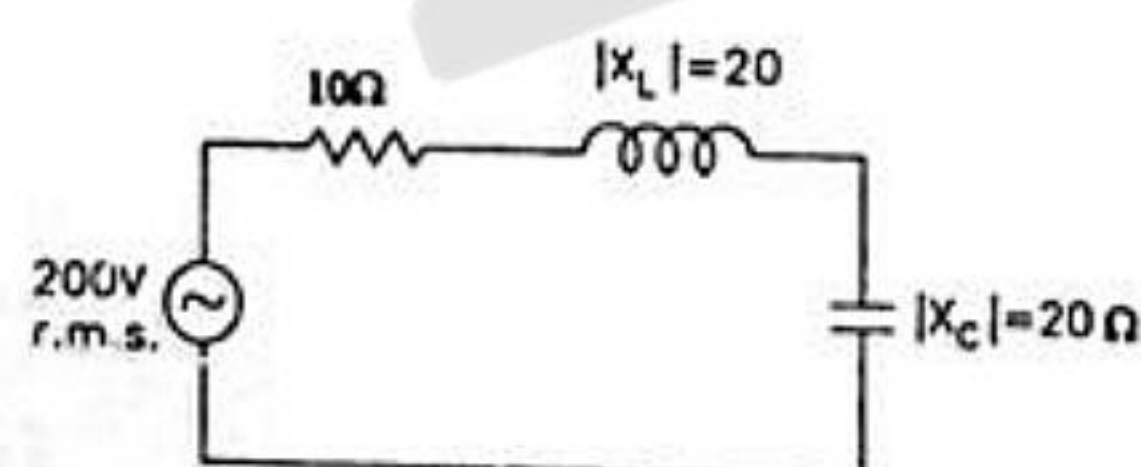
ANSWERS

- 1.1 (c) 1.2 (d) 1.3 (d) 1.4 (b) 1.5 (c) 1.6 (d) 1.7 (c) 1.8 (b) 1.9 (c) 1.10 (a)
 1.11 (b) 1.12 (d) 1.13 (c) 1.14 (d) 1.15 (a) 1.16 (c) 1.17 (b) 1.18 (c) 1.19 (a)

EXPLANATIONS

1.3 Voltage across the capacitor

$$\begin{aligned} &= \frac{200}{\sqrt{R^2 + (X_L - X_C)^2}} \times (-jX_C) \\ &= \frac{200}{\sqrt{100 + (20 - 20)^2}} \times (-j20) \\ &= -j400 \\ &= 400 \angle -90^\circ \text{ V} \end{aligned}$$



1.4 In the Laplace domain,

$$V_o(s) = \frac{V_i(s)}{R + \frac{1}{Cs}} \times R$$

$$= \frac{V_i(s) RCs}{RCs + 1}$$

$$V_i(t) = 100 t u(t)$$

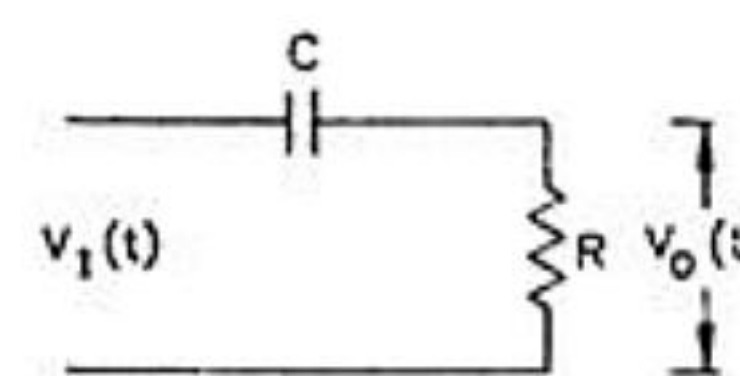
and $V_i(s) = \frac{100}{s^2}$

Hence, $V_o(s) = \frac{100}{s^2} \left[\frac{5 \times 10^3 \times 10^{-6} s}{5 \times 10^3 \times 4 \times 10^{-6} s + 1} \right]$

$$= \frac{2}{s(2 \times 10^{-2} s + 1)} \approx \frac{2}{s}$$

$$V_o(t) = 2 u(t)$$

Maximum voltage = 2 V



1.5

$$H(s) = \frac{\omega_n^2}{s^2 + 2\zeta \omega_n s + \omega_n^2}$$

$$H(j\omega) = \frac{\omega_n^2}{-\omega^2 + 2\zeta \omega_n j\omega + \omega_n^2}$$

$$|H(j\omega)| = \frac{\omega_n^2}{\sqrt{(\omega_n^2 - \omega^2)^2 + (2\zeta \omega_n \omega)^2}}$$

$$|H(j0)| = 1$$

If ω_c is the 3-dB frequency, then

$$\begin{aligned} |H(j\omega_c)| &= \frac{\omega_n^2}{\sqrt{(\omega_n^2 - \omega_c^2)^2 + (2\zeta \omega_n \omega_c)^2}} \\ &= 0.707 \end{aligned}$$